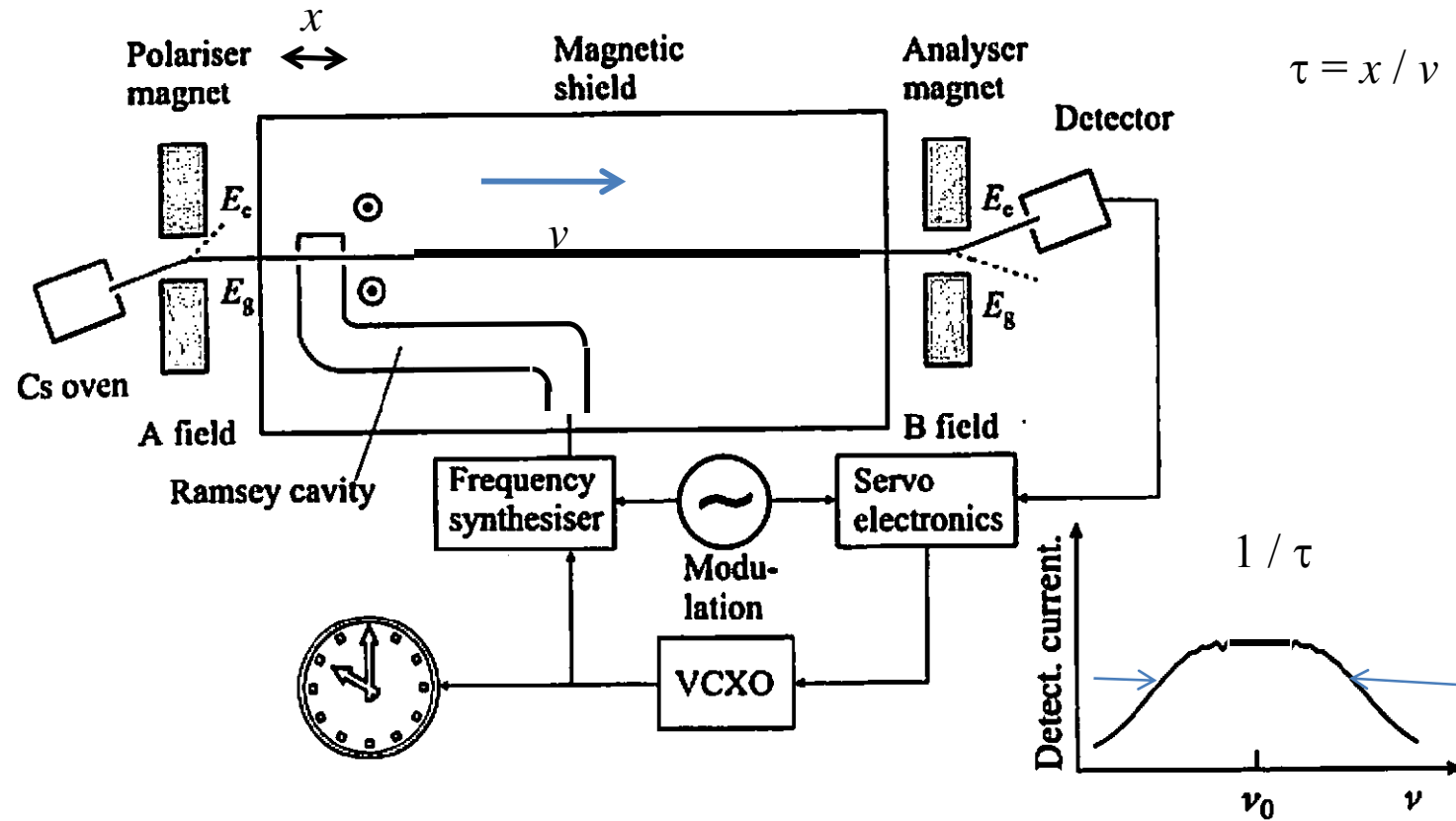


# Atomic Frequency Standards

NICT Space-Time Standards Group

Tetsuya Ido

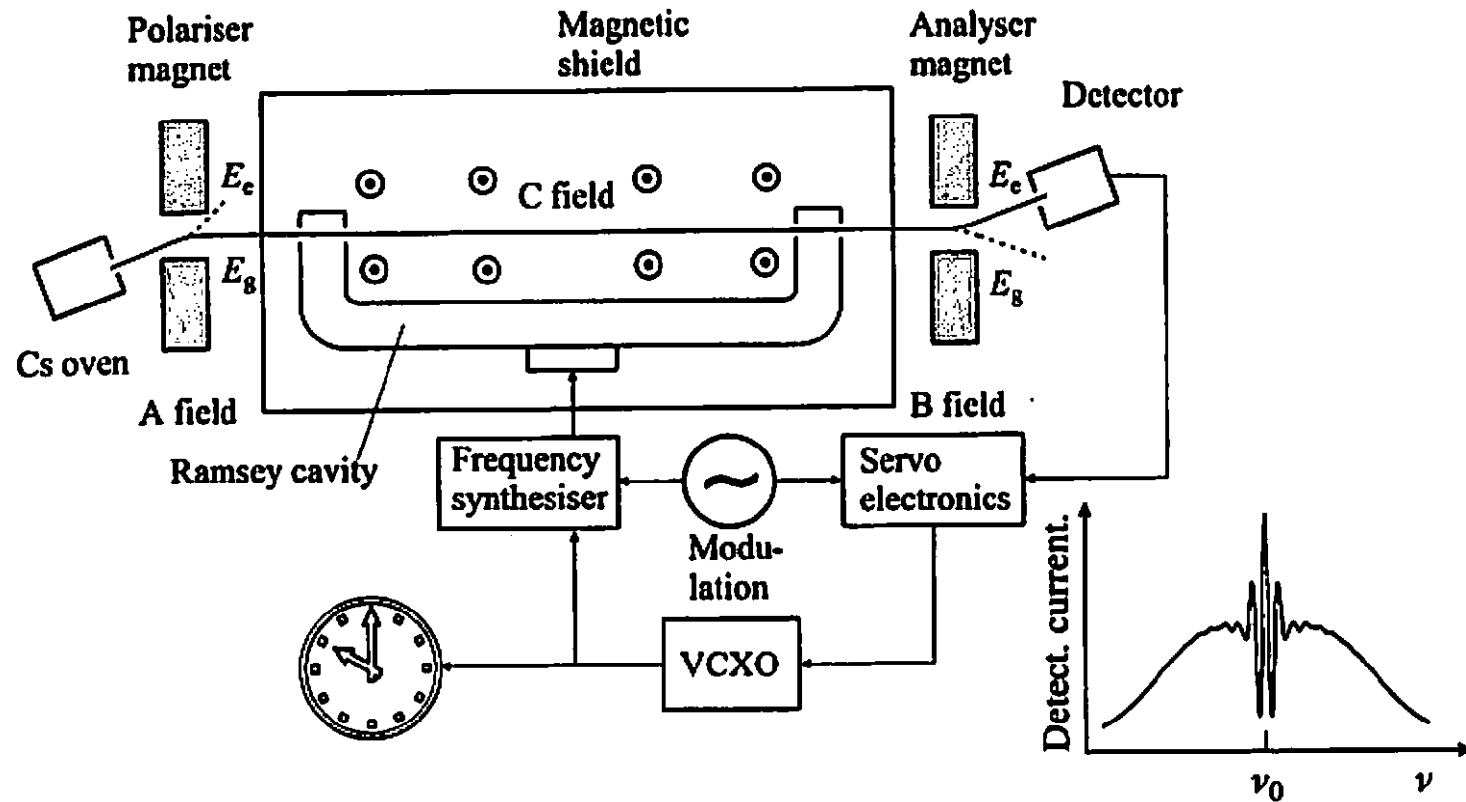
# Clock using real Cs



**Figure 7.3:** Schematic layout of a commercial Cs atomic clock. The magnetic quantisation field (C field) is perpendicular to the paper plain. The inset shows the detector current when the frequency of the synthesiser is tuned across the atomic resonance displaying the Ramsey resonance on the Rabi pedestal.

As longer time atom interacts with RF, the width will be narrower.

# Cs beam clock



**Figure 7.3:** Schematic layout of a commercial Cs atomic clock. The magnetic quantisation field (C field) is perpendicular to the paper plain. The inset shows the detector current when the frequency of the synthesiser is tuned across the atomic resonance displaying the Ramsey resonance on the Rabi pedestal.

# Optically-pumped Cesium Beam clock

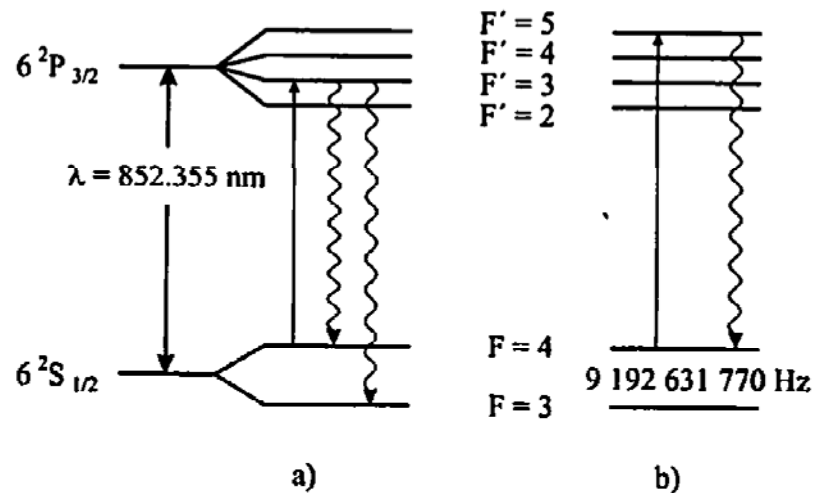


Figure 7.8: A simple version of optical pumping of a Cs atomic clock for state preparation.

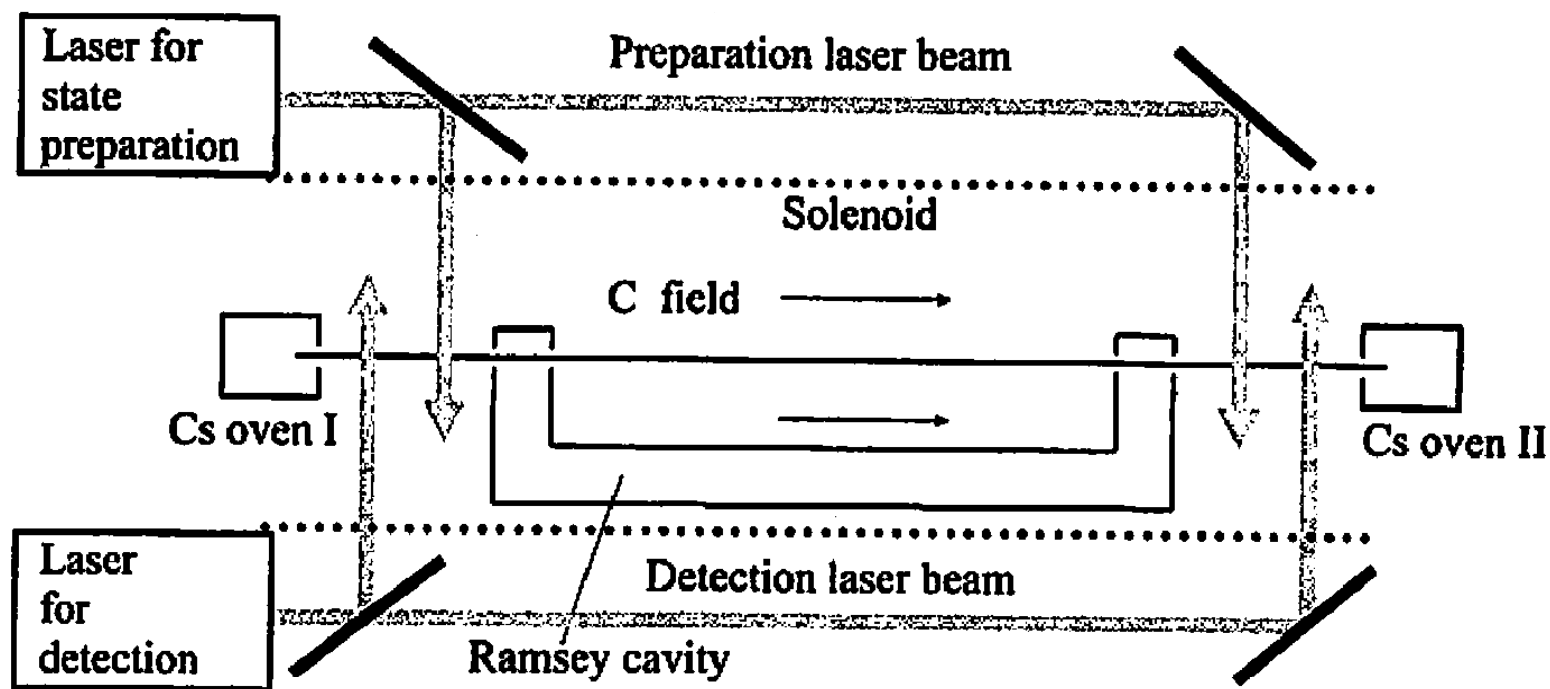


Figure 7.9: Simplified set-up of a Cs atomic clock with optical state selection and detection.

# Cs fountain clock

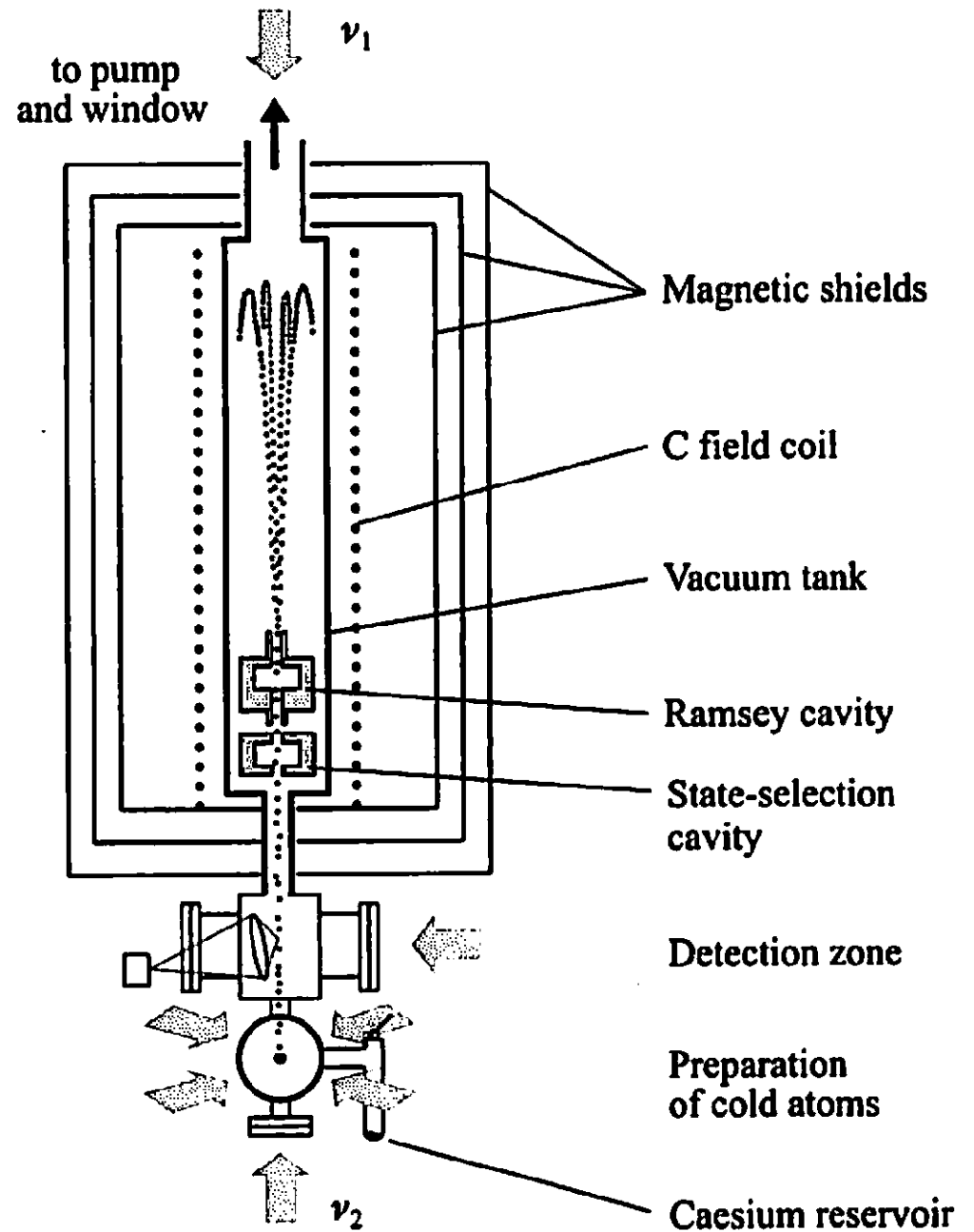
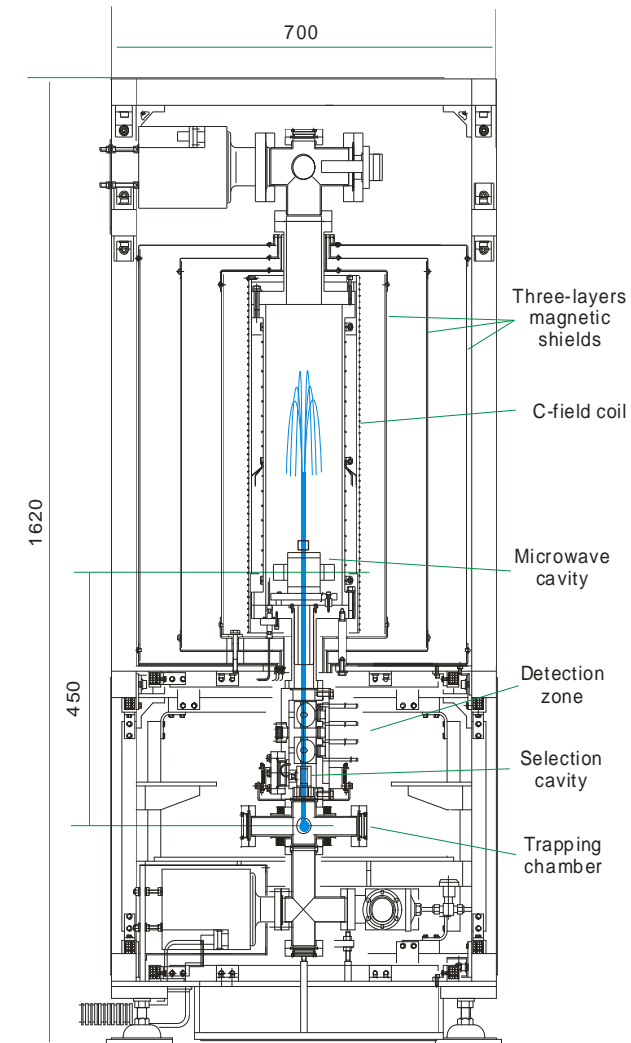


Figure 7.10: Set-up of an atomic fountain clock.

# Cesium Atomic Fountain NICT-CsF1 (2)



Captured by MOT in (0,0,1) cooling geometry

State-select just above laser cooling region

Rectangular cavity for state-selection

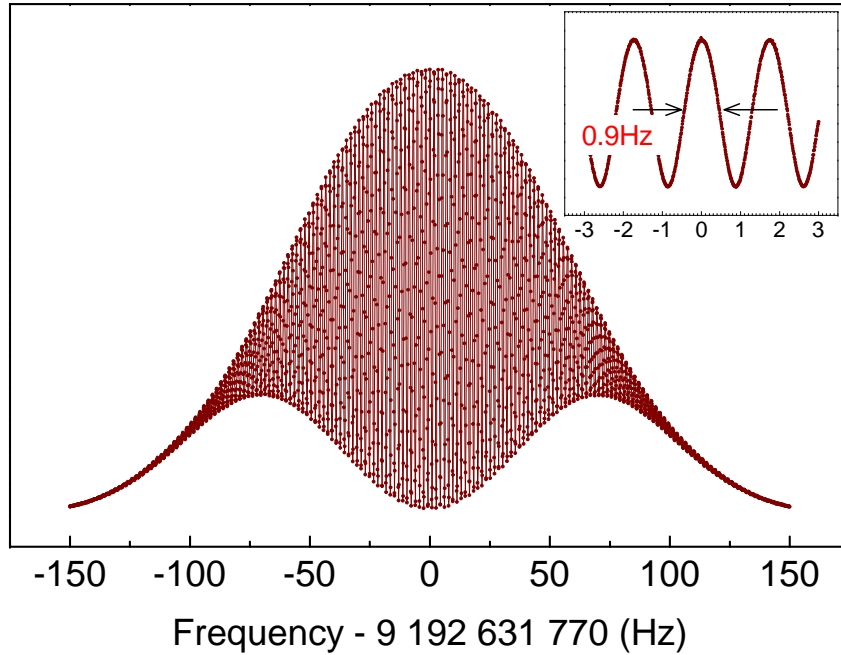
Cylindrical cavity for Ramsey resonance

Detection region above laser cooling region

Three-layers magnetic shield

Ultra high vacuum of less than  $2 \times 10^{-7}$  Pa

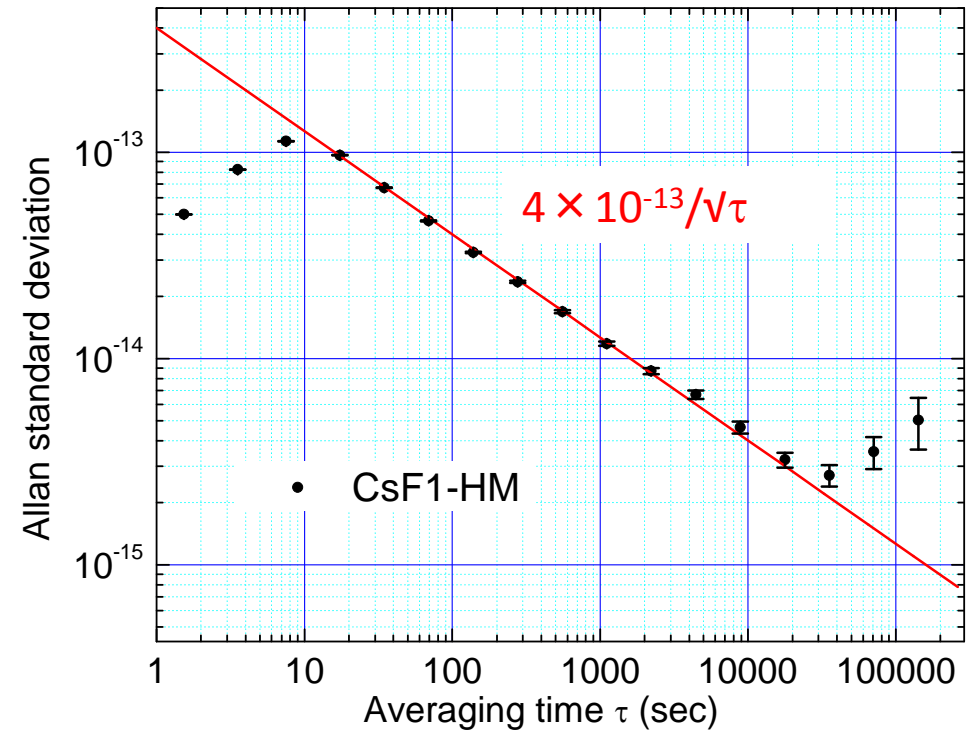
# Frequency Stability of NICT-CsF1



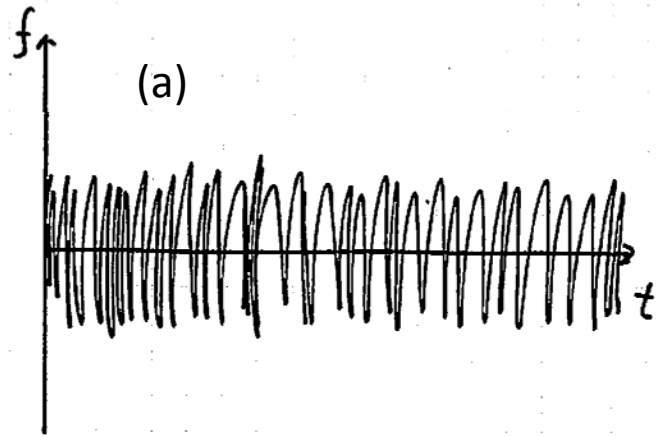
冷却温度:  $1 \sim 2 \mu\text{K}$   
打上げ速度:  $4 \text{ m/sec}$   
打上げ高さ:  $82 \text{ cm}$   
ドリフト時間:  $570 \text{ ms}$

↓  
線幅:  $< 0.9 \text{ Hz}$

$4 \times 10^{-13} @ 1 \text{ 秒}$   
 $1.4 \times 10^{-15} @ 1 \text{ 日}$   
↓  
1日前と1日後では  $1.4 \times 10^{-15}$   
しか値はずれない

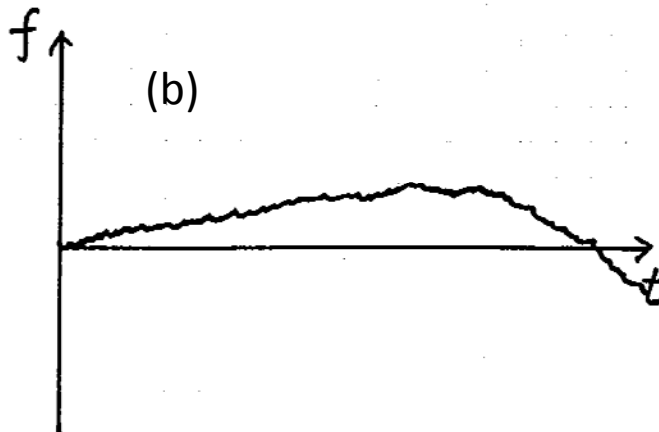


# Which oscillator do you like?



(b) Is drifting, but (a) is not.  
Then, obviously (a)?

Cs clock



But we often say (a) is noisy and (b) is smooth.

H-maser



# Hydrogen maser

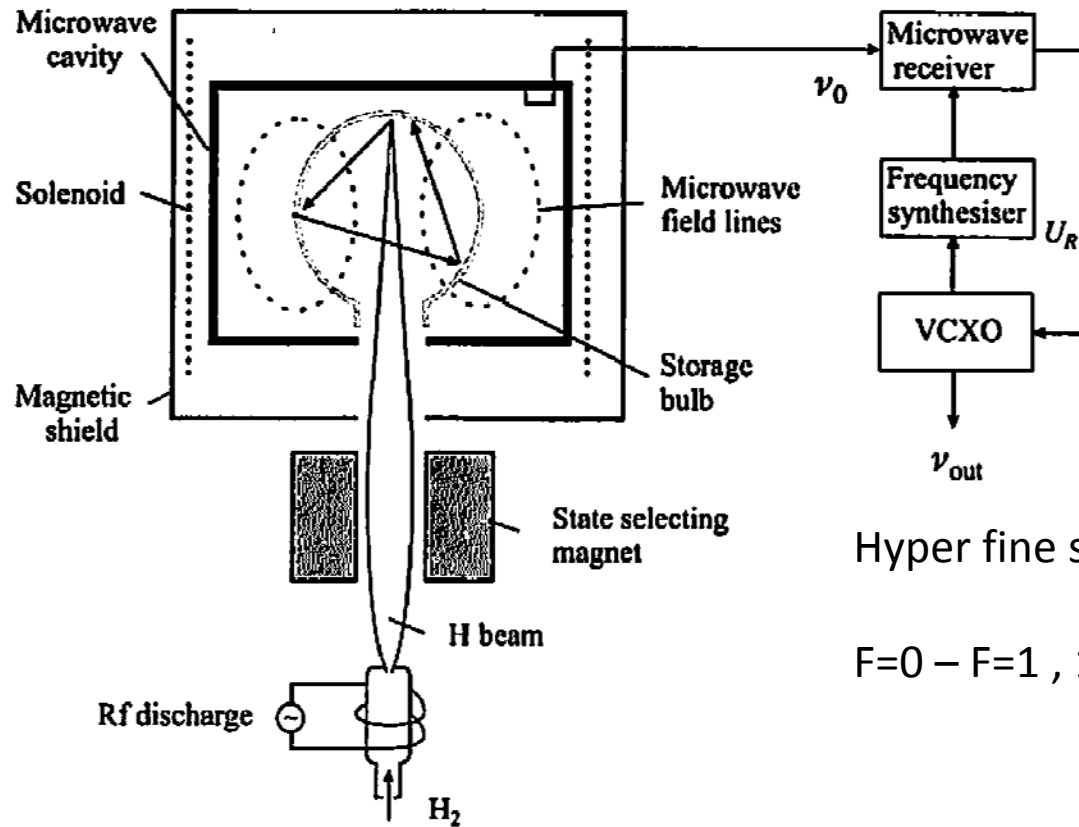


Figure 8.1: Schematic of an active hydrogen maser.

Hyper fine splitting of hydrogen

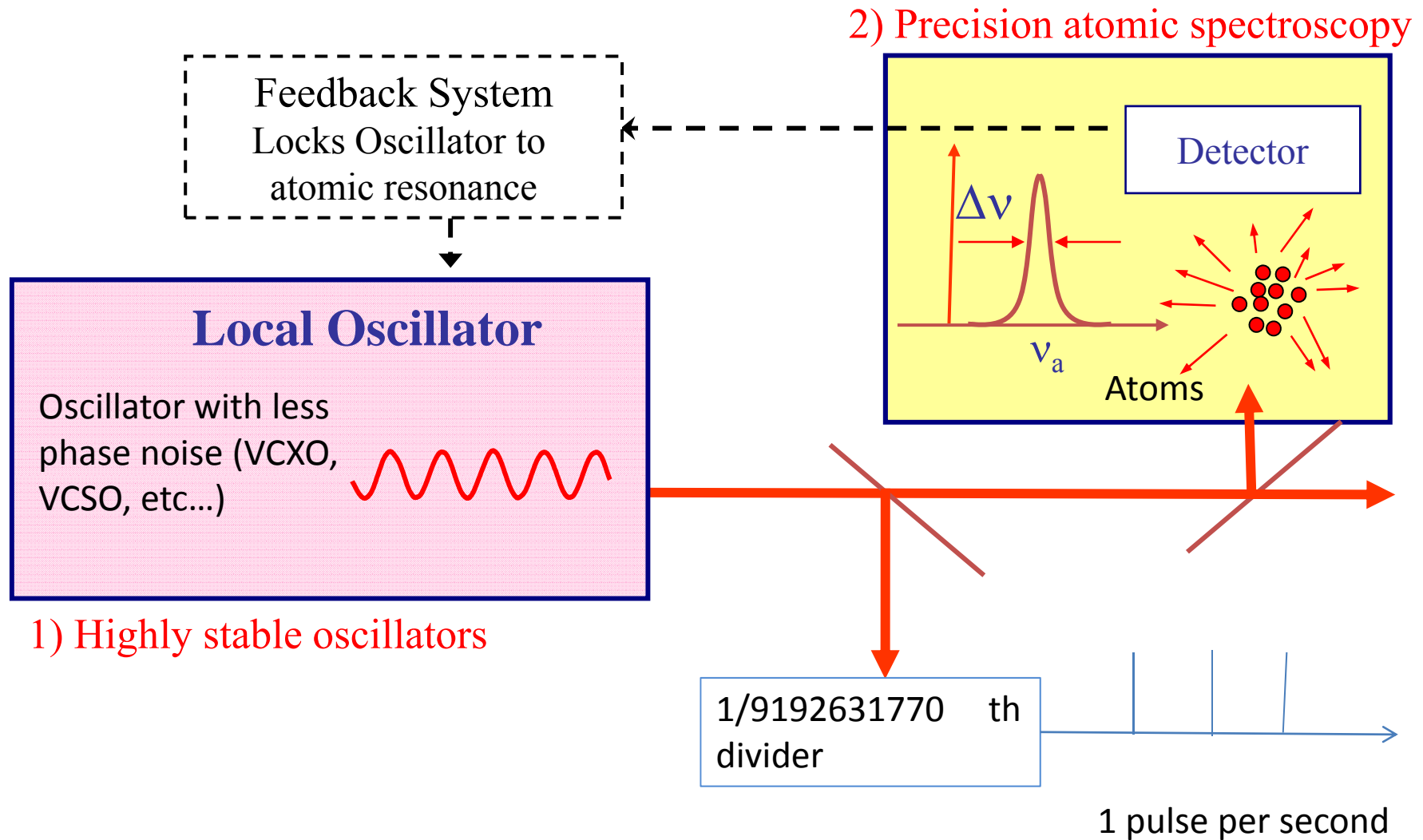
$F=0 - F=1$  , 1.42GHz

Active clock

Oscillator = standards

All Cs clock are passive. Source oscillator does not have Cs inside.

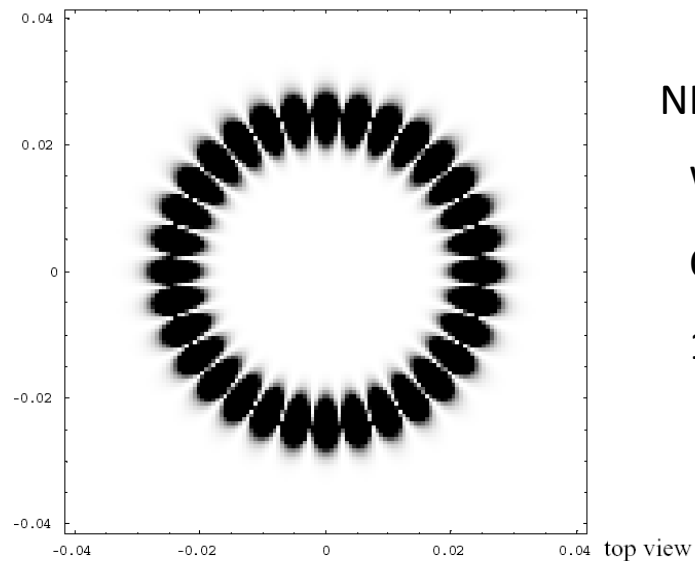
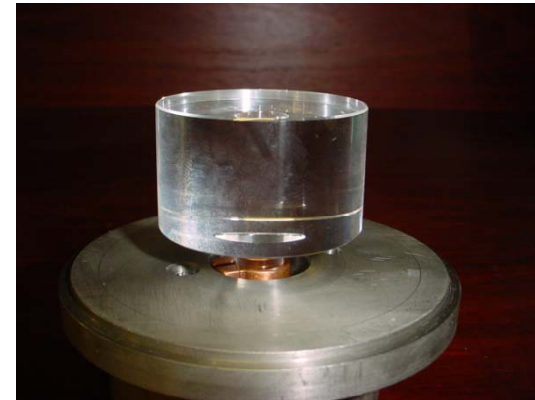
# Components of passive clock



**Local oscillator for microwave clock**

# Cryogenic Sapphire Oscillator

- Sapphire crystal inside liquid helium
- Whispering Gallery Mode
- Q-value =  $10^9$
- Narrow BPF



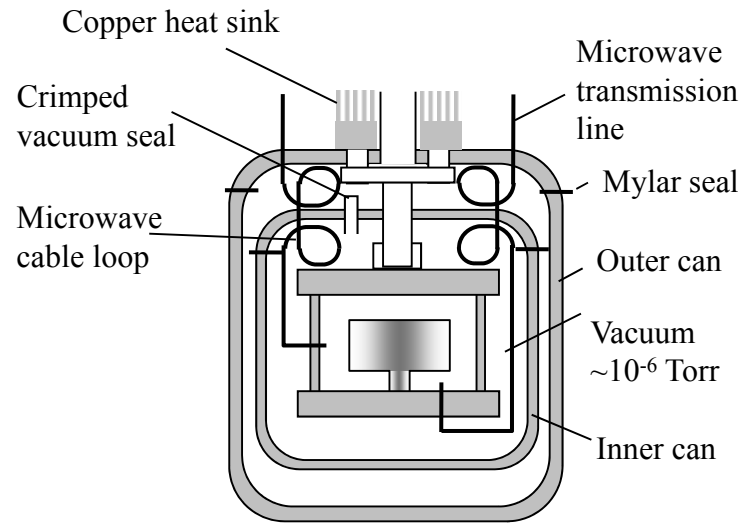
NICTのCSO

WGH<sub>16,0,0</sub>

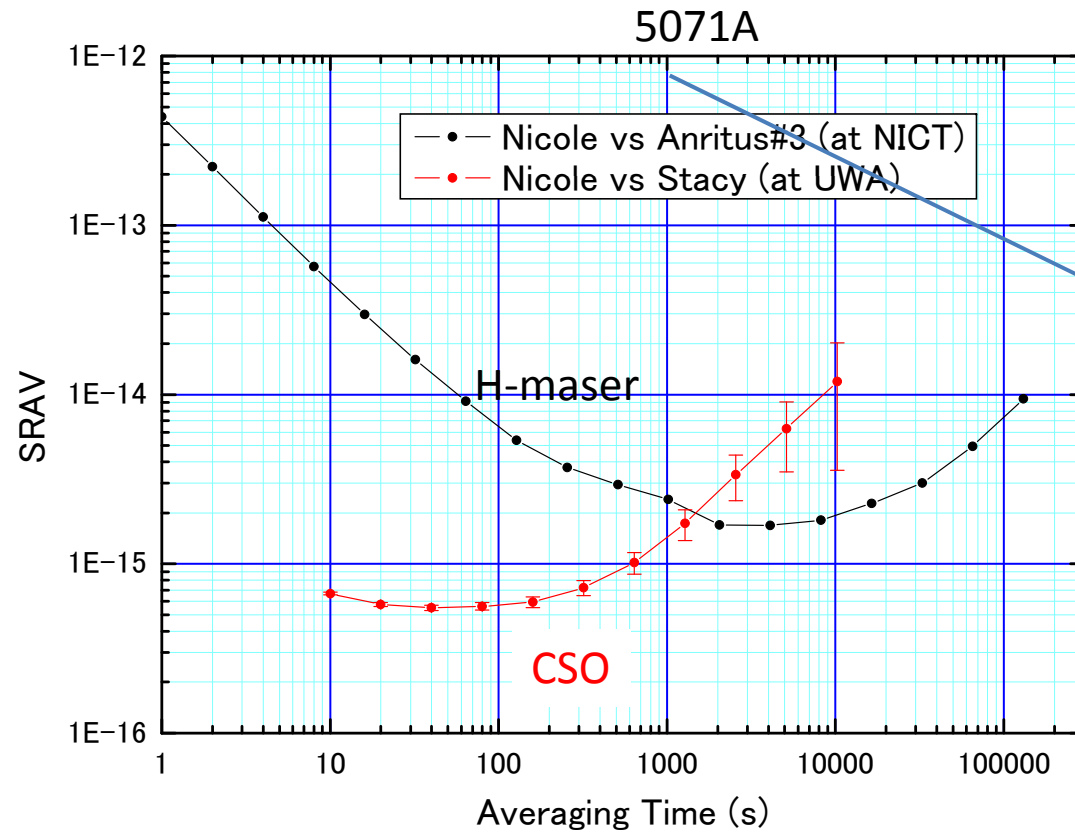
Q-value =  $1.7 \times 10^9$

11.2005GHz@7K

# NICT-CSO(1)

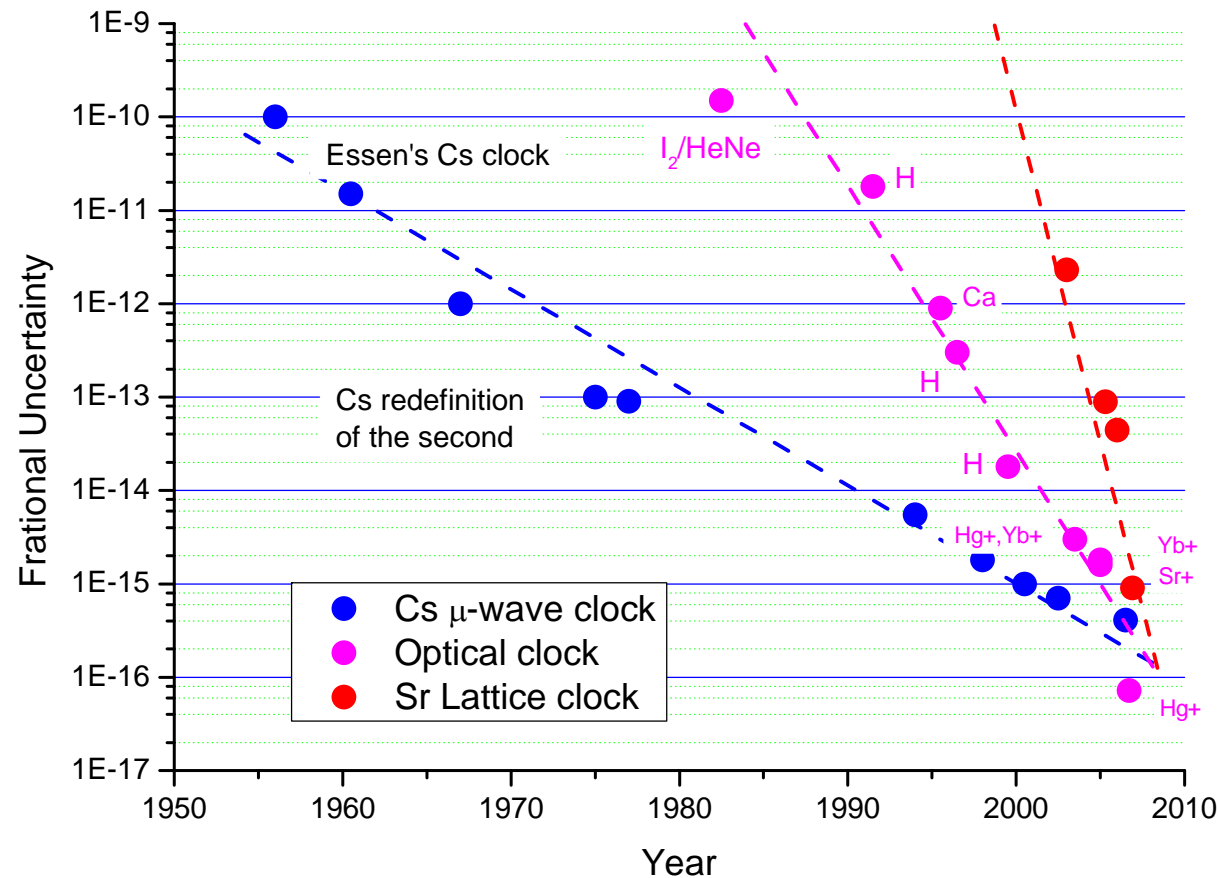


# NICT-CSO



# Optical Clocks

## Accuracy: Optical clock now comparable or even better than Cs

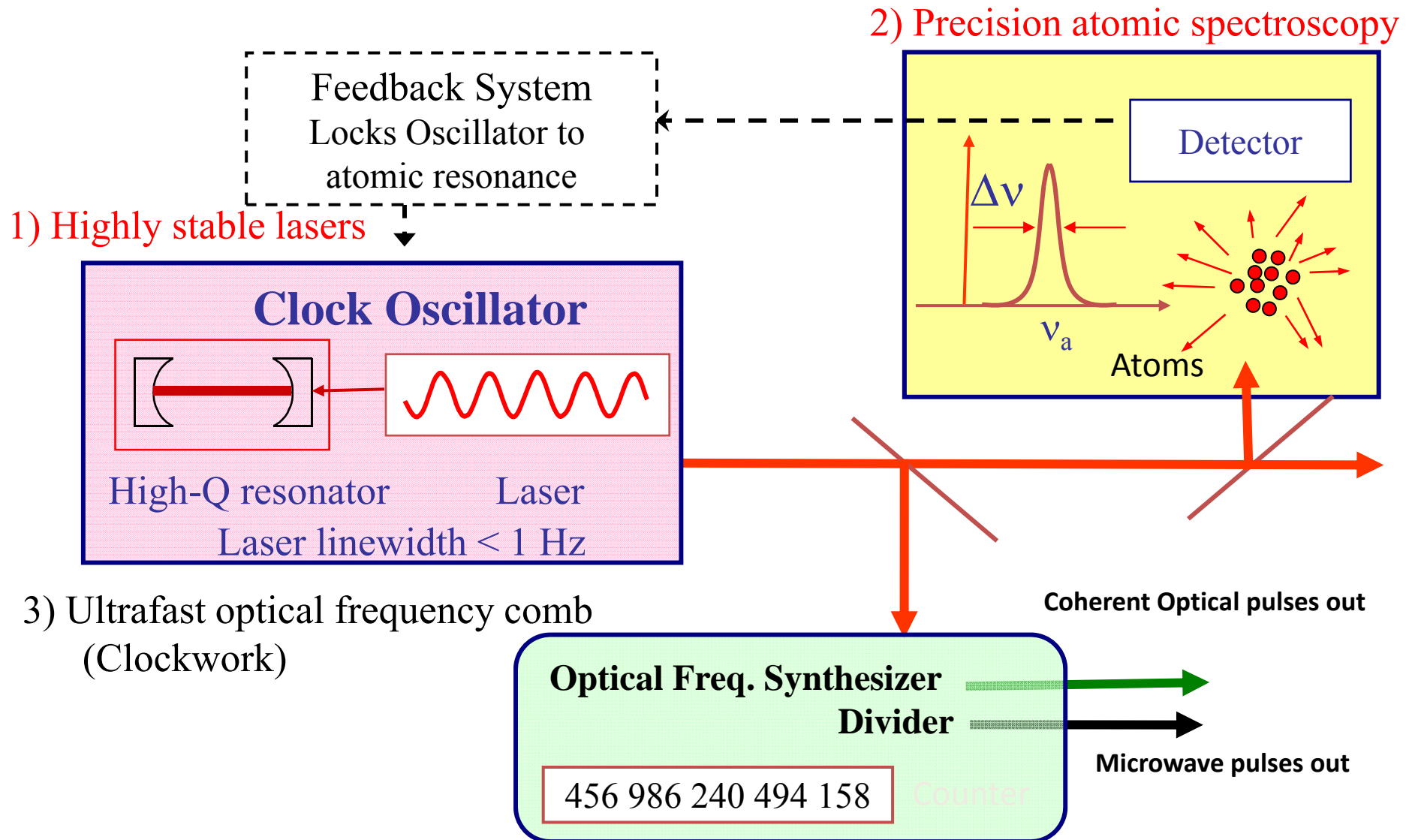


- Now a Hg ion has better accuracy than Cs.
- Short time Instability: Cs > ions > lattice clock
- Are lattice clocks really promising?

My talk could be biased to lattice clocks to introduce ideas and latest results



# Optical Clock Components



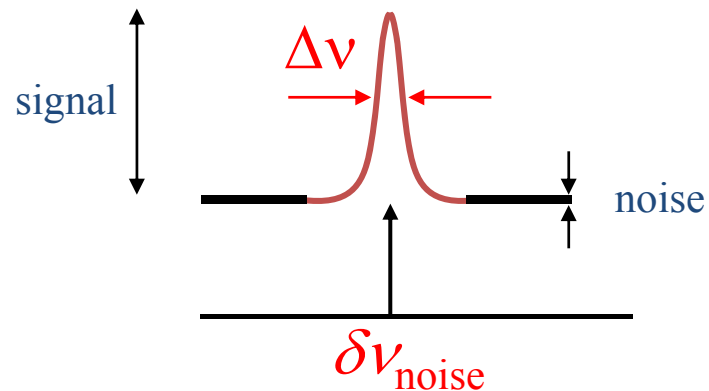
# **Atomic References**

## **Ion and neutral atoms**

# Optical Frequency Standards

## sensitivity and resolution

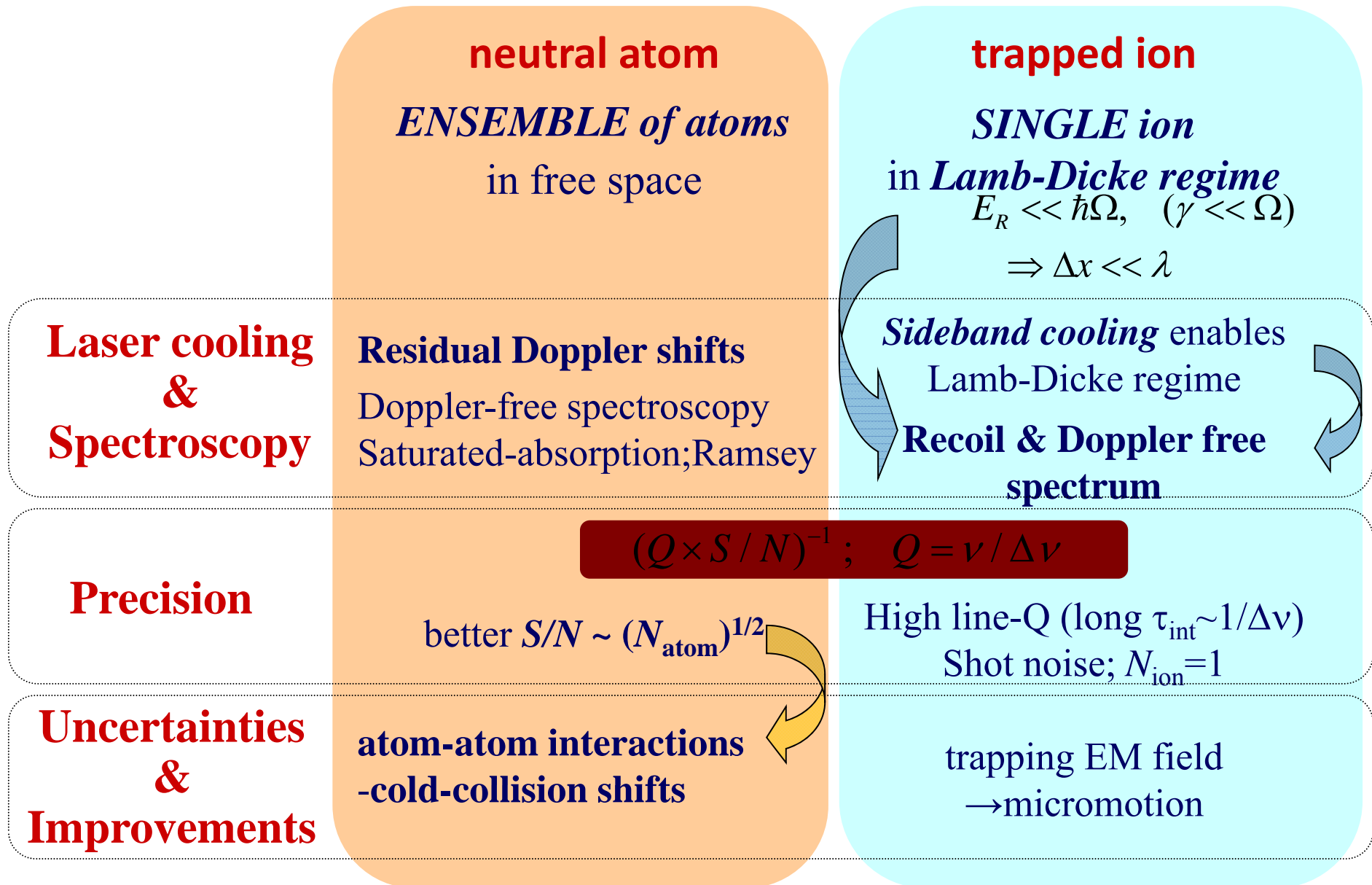
High line Q & good signal-to-noise ratio (stability)



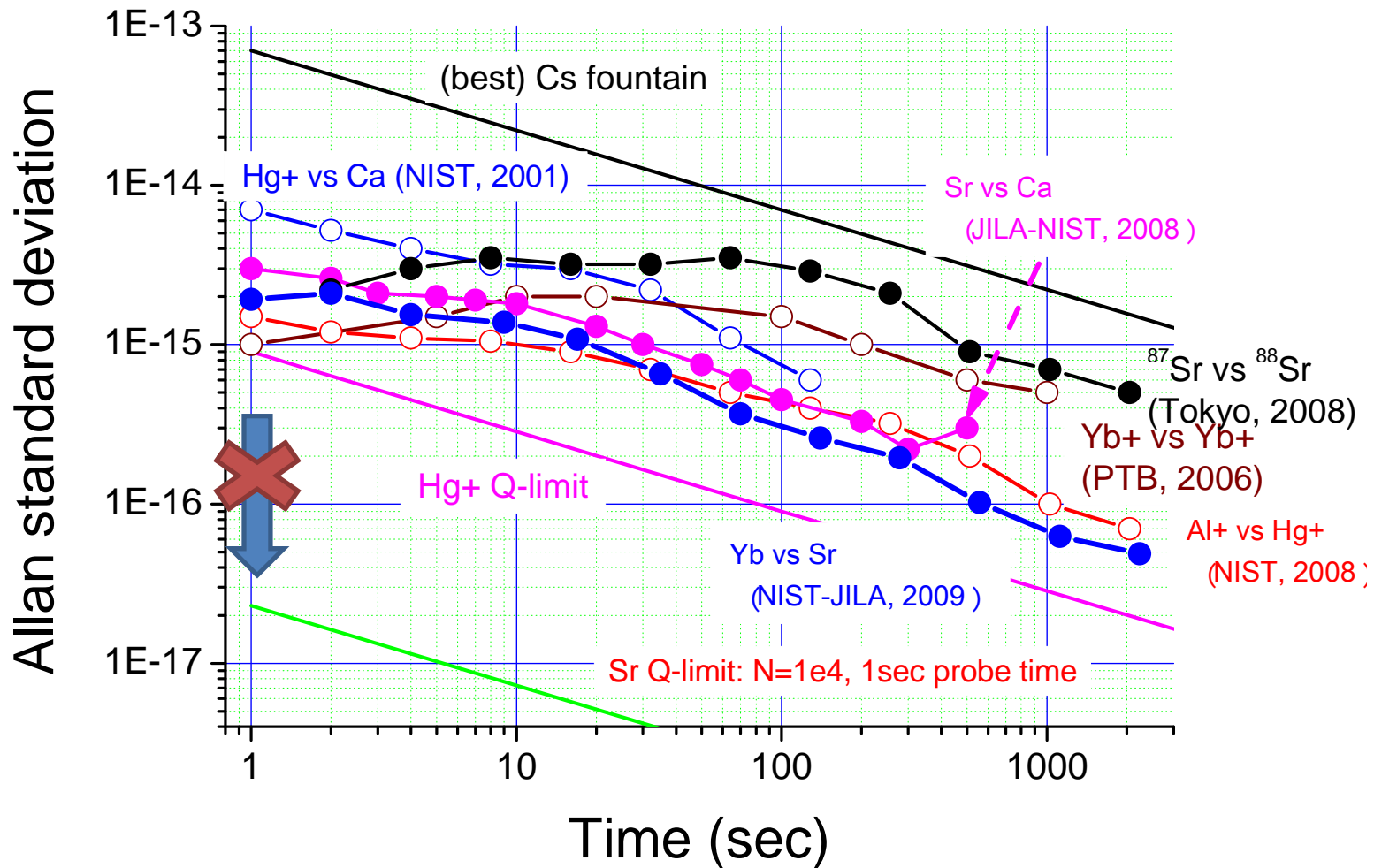
$$\delta\nu_{noise} \approx \frac{\Delta\nu (FWHM)}{(S/N)|_{\tau}} \longrightarrow \frac{\delta\nu_{noise}}{\nu_0} \approx \frac{1}{Q} \cdot \frac{1}{S/N} \cdot \frac{1}{\sqrt{\tau}}, \quad Q \approx \nu_0 / \Delta\nu$$

Increase S/N, or Q, by 10,  $\longrightarrow$  decrease waiting time by 100

# neutral vs. ion optical-standards (*before lattice clock*)



# Optical atomic clocks



- Comparison with other clocks is necessary to know the stability
- $(\text{Averaging time})^{-1/2}$  dependence
- Short time stability limited by laser spectral width

# Single ion Clocks

# Single Ions in Paul Traps: state-of-the-art optical clocks



Very low uncertainty is possible (to  $10^{-18}$ )  
proposed by Hans Dehmelt 1975

“Alkali-like” ions

S-D Q-pole trans.

Natural width:  $\sim$ Hz...

Hg<sup>+</sup> (NIST)

Yb<sup>+</sup> (PTB, NPL)

Sr<sup>+</sup> (NPL, NRC)

Ca<sup>+</sup> (Mars., Innsb., NICT)

Ba<sup>+</sup> (U Wash.)

- Quadrupole shift
- Broader natural linewidth ( $\sim$ Hz)

“Alkaline earth-like” ions

$^1S_0$ - $^3P_0$  doubly forbidden

Natural width:  $\sim$ mHz!!

In<sup>+</sup> (NICT?, )

Al<sup>+</sup> (NIST)

- Strong transitions from ground states locate in VUV region  
→ Schemes of cooling and detection needed

# Recent progress of ion clocks

## Alkaline earth-like ions

### Spectroscopy Using Quantum Logic

P. O. Schmidt,\*† T. Rosenband, C. Langer, W. M. Itano,  
J. C. Bergquist, D. J. Wineland

Excited state population of Al<sup>+</sup> was effectively copied to Be<sup>+</sup> which has a good “detection” transition

P. Schmidt, *Science* **309** 749 (2005)

**Ion clocks became available for intrinsically ultranarrow transitions, and currently NIST Al<sup>+</sup> clock reaches 1e-17 level**

*Rosenband, Science* **319**, 1808 (2008);

Al<sup>+</sup>:  $^1S_0$ - $^3P_0$

Natural linewidth: ~mHz  
Insensitive to black body radiation



# Lattice Clocks

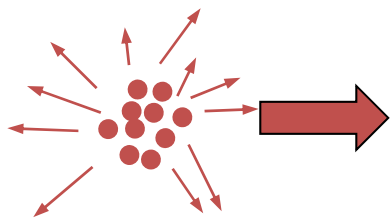
# We can be picky!

## That's a lattice clock

### Free Neutral Atoms (Stability)

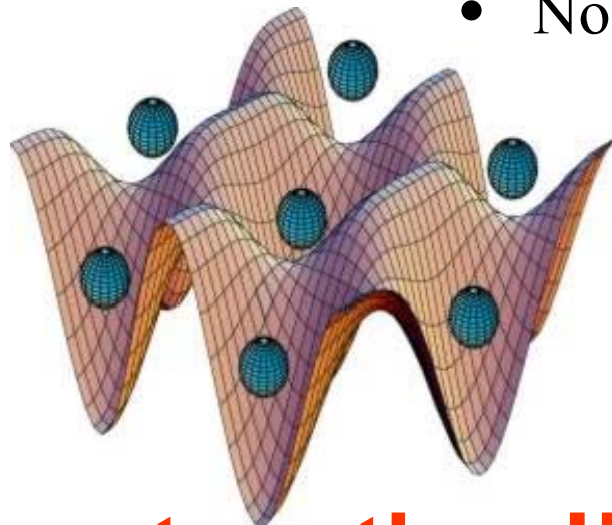
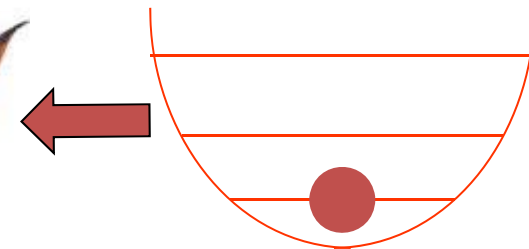
- Many Quantum Absorbers
  - Large N

$$\text{stability} \propto \sqrt{N}$$



### Single Trapped Ion (Accuracy)

- Tight Confinement
  - No Doppler
  - Long Interrogation Times
- No Collisions



**Merge together !!**

# Simultaneous control of induced dipole potentials for cooling transition

A strong laser light couples states *connected by dipole transitions*.  
Cooling ground & excited states can be controlled *independently*.

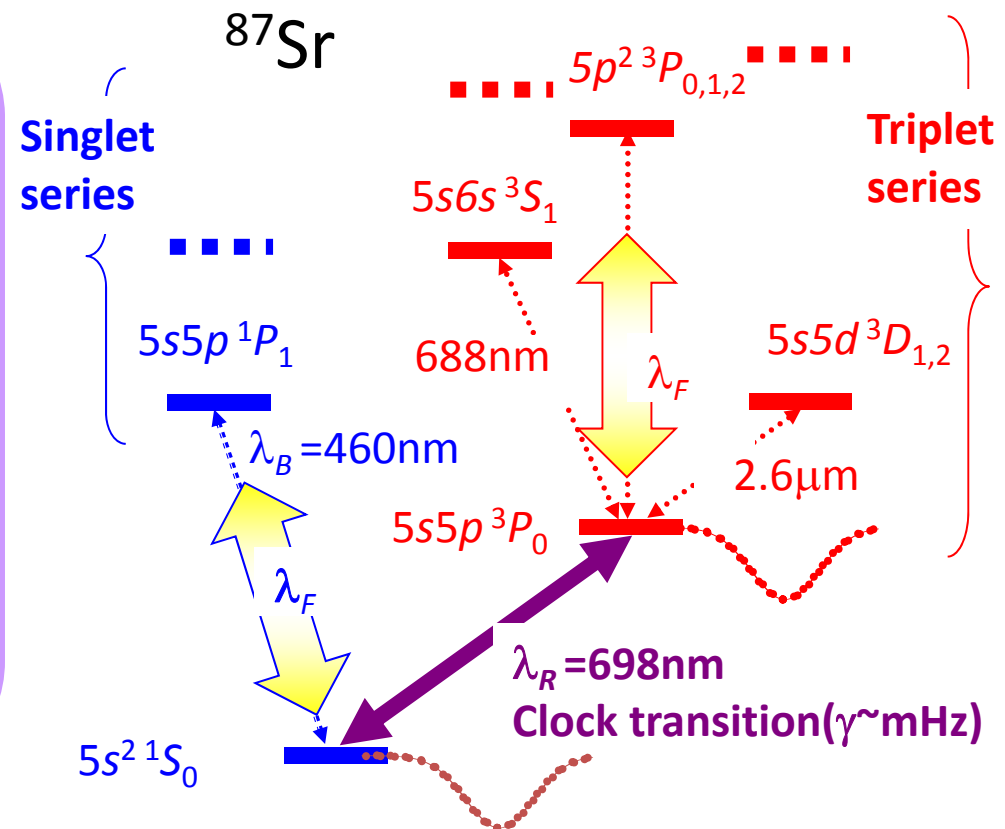
induced polarizability

$$\alpha_n(\omega) = -\frac{2}{\hbar} \sum_m \frac{\omega_{nm} |\mu_{nm}|^2}{\omega_{nm}^2 - \omega^2}$$

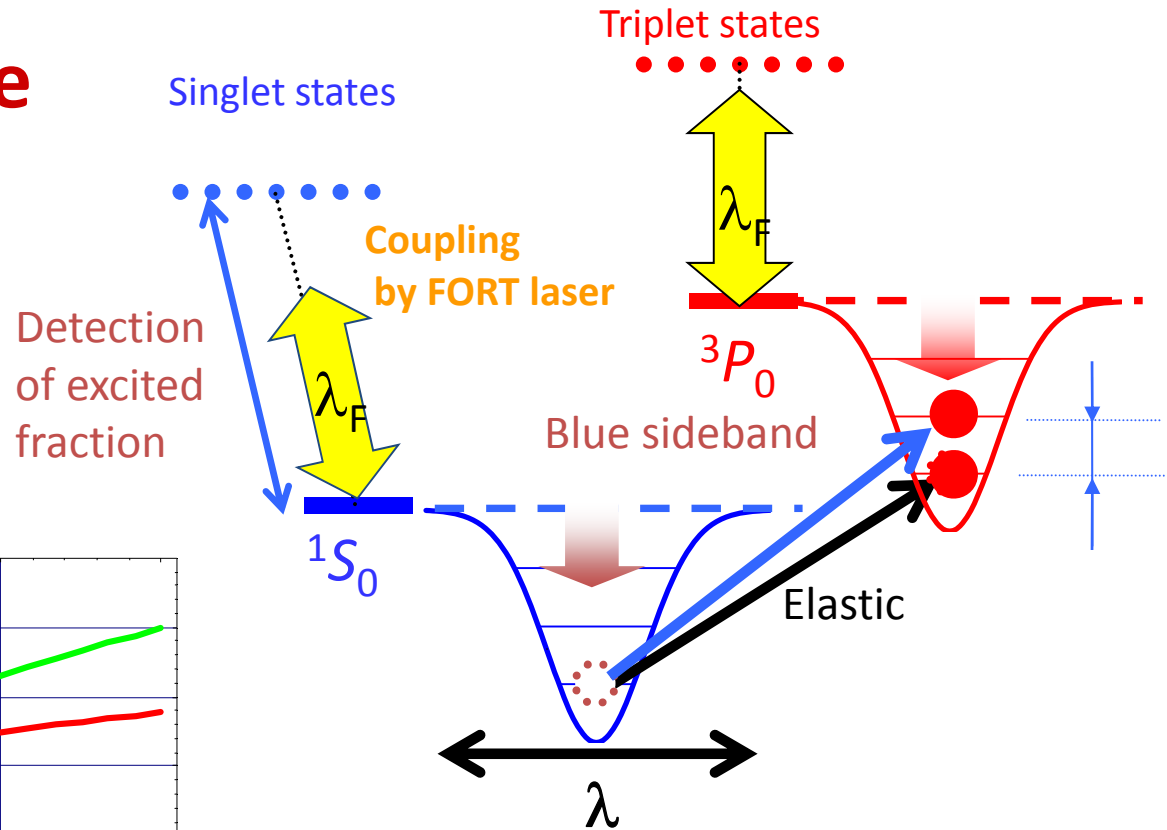
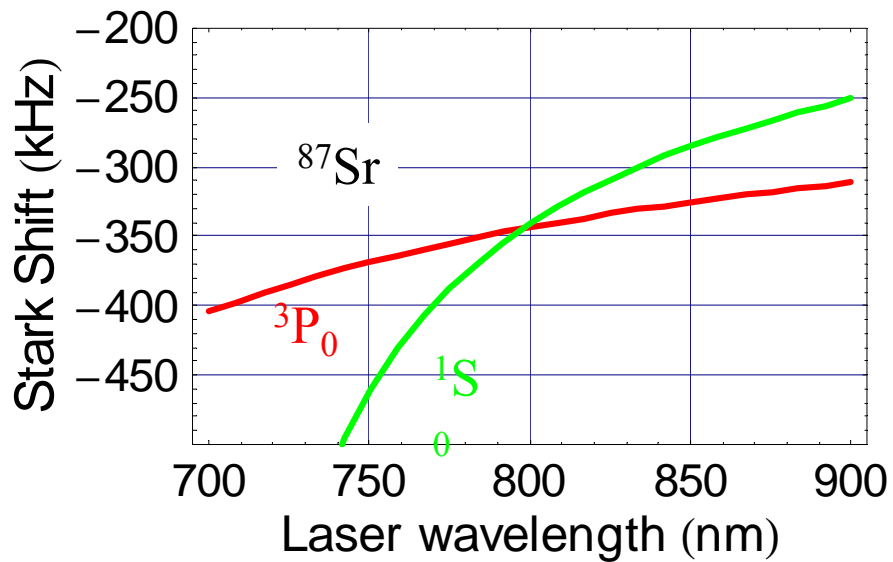
$$\hbar\omega_{nm} = E_n - E_m$$

light shift potential

$$U_n(r, \omega) = -\frac{1}{4} \alpha_n(\omega) |E(r, \omega)|^2$$



# State insensitive optical lattice

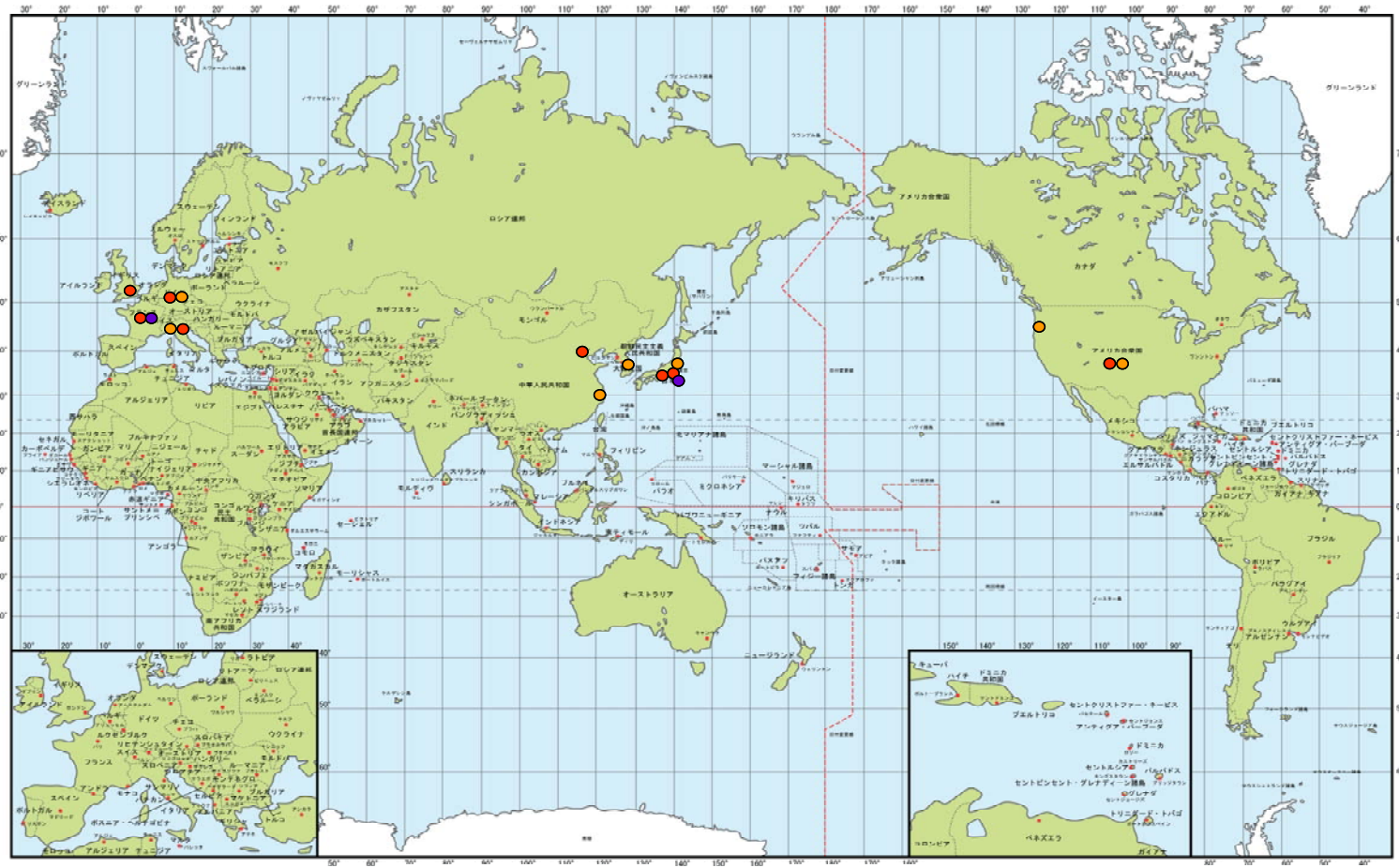


		Magic $\lambda$	
Sr	$^1S_0$ - $^3P_1$	914nm	JST, JILA
Sr	$^1S_0$ - $^3P_0$	813nm	Tokyo, JILA, SYRTE, NICT
Yb	$^1S_0$ - $^3P_1$	759nm	NIST, AIST
Hg	$^1S_0$ - $^3P_0$	358nm	Tokyo, SYRTE

Katori *et al.*, Phys. Rev. Lett. 91, 173005 (2003).

# Optical lattice clock

## Worldwide spread



- strontium
- ytterbium
- mercury

# List of optical radiation to express meter

$\lambda$		frequency	uncertainty
237 nm	$^{115}\text{In}^+$ , $5s^2\ ^1S_0 - 5s5p\ ^3P_0$ transition	1267402452899.92 kHz	$3.6 \times 10^{-13}$
243 nm	$^1\text{H}$ , $1S - 2S$ , 2 photon transition	1233030706593.55 kHz	$2.0 \times 10^{-13}$
282 nm	$^{199}\text{Hg}^+$ , $5d^{10}6s\ ^2S_{1/2} (F=0) - 5d^96s^2\ ^2D_{5/2} (F=2)$ transition	1064721609899145 Hz	$3 \times 10^{-15}$
436 nm	$^{171}\text{Yb}^+$ , $6s^2S_{1/2} (F=0) - 5d^2D_{3/2} (F=2)$ transition	688358979309308 Hz	$9 \times 10^{-15}$
467 nm	$^{171}\text{Yb}^+$ , $^2S_{1/2} (F=0) - ^2F_{7/2} (F=3)$ transition	642121496772657 Hz	$6 \times 10^{-14}$
532 nm	Nd:YAG laser, $^{127}\text{I}_2$ , R(56)32-0:a <sub>10</sub>	563260223513 kHz	$8.9 \times 10^{-12}$
543 nm	He-Ne laser, $^{127}\text{I}_2$ , R(106)28-8:b <sub>10</sub>	551580162400 kHz	$4.5 \times 10^{-11}$
578 nm	$^{171}\text{Yb}$ , $6s^2\ ^1S_0 (F=1/2) - 6s6p\ ^3P_0 (F=1/2)$ transition	518295836590864 Hz	$1.6 \times 10^{-13}$
633 nm	He-Ne laser, $^{127}\text{I}_2$ , R(127)11-5:a <sub>16</sub>	473612353604 kHz	$2.1 \times 10^{-11}$
657 nm	$^{40}\text{Ca}$ , $^1S_0 - ^3P_1$ , $\Delta m_J = 0$	455986240494140 Hz	$1.8 \times 10^{-14}$
674 nm	$^{88}\text{Sr}^+$ , $5^2S_{1/2} - 4^2D_{5/2}$	444779044095484 Hz	$7 \times 10^{-15}$
698 nm	$^{87}\text{Sr}$ , $5s^2\ ^1S_0 - 5s5p\ ^3P_0$ transition	429228004229873.65 Hz	$1 \times 10^{-15}$
698 nm	$^{88}\text{Sr}$ , $5s^2\ ^1S_0 - 5s5p\ ^3P_0$ transition	429228066418012 Hz	$1 \times 10^{-14}$
729 nm	$^{40}\text{Ca}^+$ , $4s\ ^2S_{1/2} - 3d\ ^2D_{5/2}$ transition	411042129776393 Hz	$4 \times 10^{-14}$
778 nm	$^{85}\text{Rb}$ , $5S_{1/2}(F=3) - 5D_{5/2}(F=5)$ , 2 photon transition	385285142375 kHz	$1.3 \times 10^{-11}$
1.5mm	$^{13}\text{C}_2\text{H}_2$ , P(16)( $\nu_1 + \nu_3$ ) transition	194369569384 kHz	$2.6 \times 10^{-11}$
3.39mm	He-Ne laser, $\text{CH}_4$ , $n_3$ , P(7), $F_2^{(2)}$	88376181600.18 kHz	$3 \times 10^{-12}$